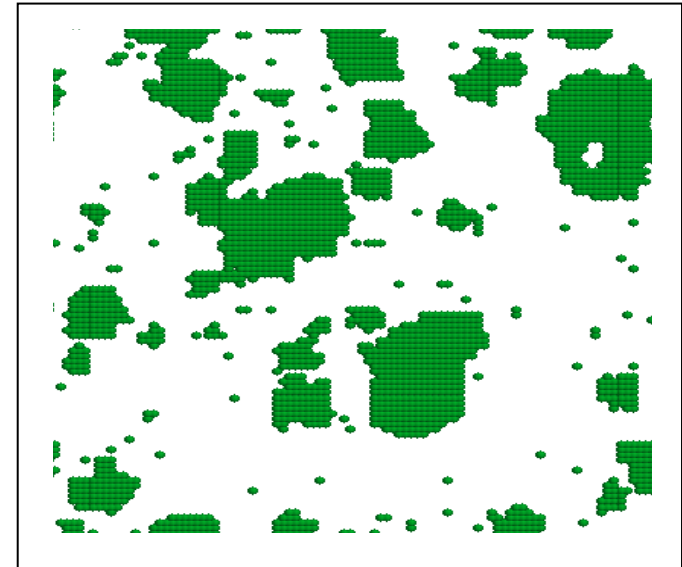
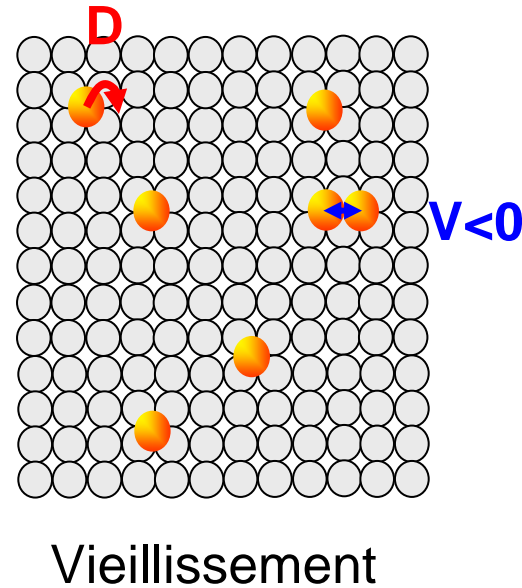
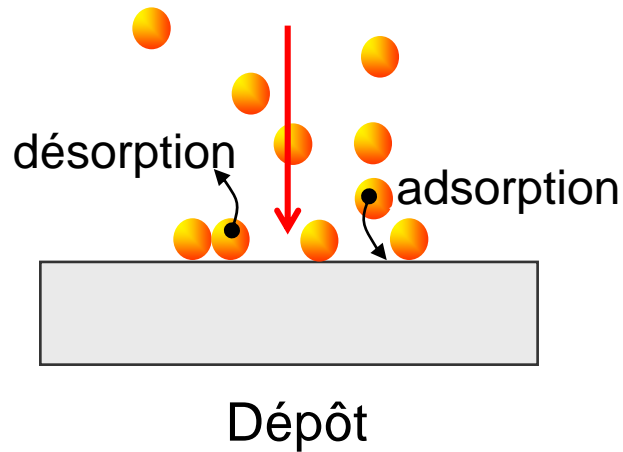


# *Dynamique d'amas et amas dynamiques*

Isabelle, Émile, Fabienne, Bernard



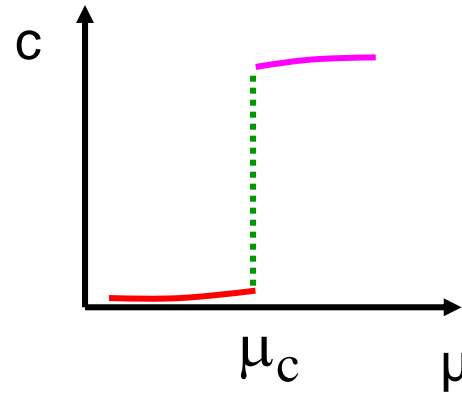
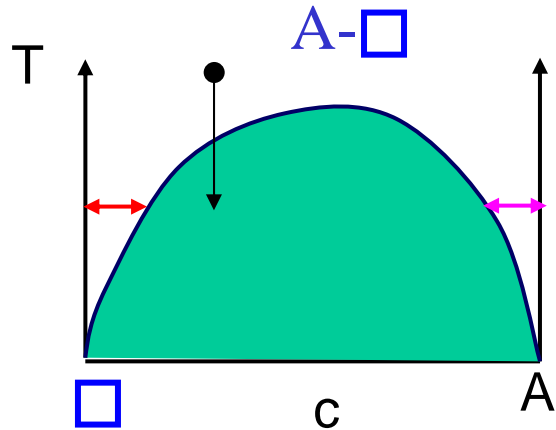
Ag/Cu (001)

# *Problématique*

---

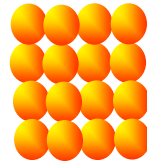
- ✓ Thermodynamique des agrégats purs
  - Energie libre des agrégats
  - Energie libre de surface des agrégats
- ✓ Agrégats au coeur des lacunes ...  
Lacunes au coeur des agrégats !
- ✓ Agrégats bimétalliques

# Energie libre de formation des agrégats



$$\frac{C_n}{D_n} = \exp\left(-\frac{\Delta F_n}{kT}\right)$$

$$\Delta F_n = F_n - n\mu$$



$$F_n = n(\underbrace{E_{\text{ads}} + ZV_{AA}/2}_{\mu_c}) + 4(\sqrt{n} - 2)\sigma_{\text{côté}} + 4\sigma_{\text{sommet}}$$

$$\mu_c$$

$$\sigma = \sigma_{\text{côté}}$$

$$\sigma' = 4\sigma_{\text{sommet}} - 8\sigma_{\text{côté}}$$

$$\Delta\mu = \mu - \mu_c$$

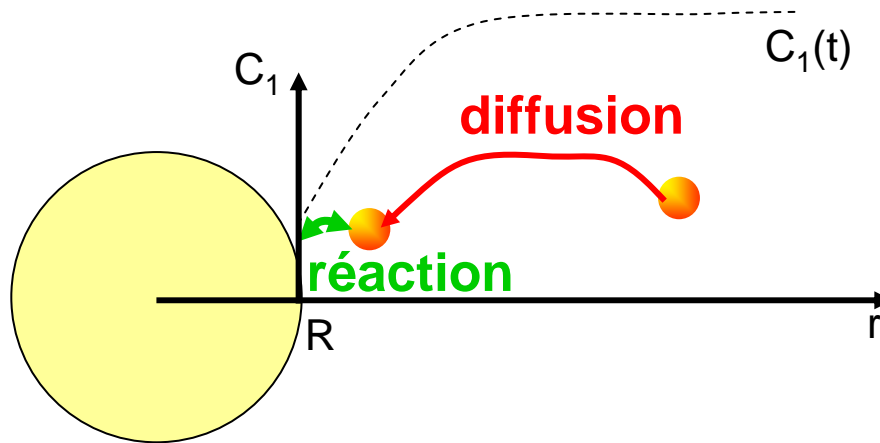
$$\Delta F_n = -n\Delta\mu + 4\sqrt{n}\sigma + \sigma'$$

# Cinétique de précipitation

$$\frac{dC_n(t)}{dt} = \beta_{n-1} \frac{D_n}{D_{n-1}} C_{n-1}(t) - \left( \alpha_n D_1 + \beta_n \frac{D_{n+1}}{D_n} \right) C_n(t) + \alpha_{n+1} D_1 C_{n+1}(t)$$

$$D_n = 1$$

$$\beta_n, \alpha_n = ?$$



$$C_I = 0$$

$$C_I = C_1$$

$$\beta_n = \frac{dn}{dt} = 2\pi R \left| -D(\nabla C_1)_R \right|$$

$$\frac{dn}{dt} = \beta_n C_I - \alpha_n (1 - C_I)$$

**Cinétique limitée par la diffusion**

**Cinétique limitée par la réaction**

# Energie libre de surface des agrégats

---

$$\beta_n = k_n C_1$$

Diffusion, indépendant de la thermo

état stationnaire  $\Leftrightarrow$  état d'équilibre

$$\frac{dC_n}{dt} = 0 \Rightarrow C_{n+1} \alpha_{n+1} = C_n \beta_n$$

$$D_n = 1$$


$$\alpha_{n+1} = \beta_n \exp\left(-\frac{\Delta F_{n+1} - \Delta F_n}{kT}\right) = k_n C_1 \exp\left(\frac{4\sigma(\sqrt{n+1} - \sqrt{n}) - \Delta\mu}{kT}\right)$$

**nécessite la connaissance de  $\Delta F_n$  ou de  $\sigma$**

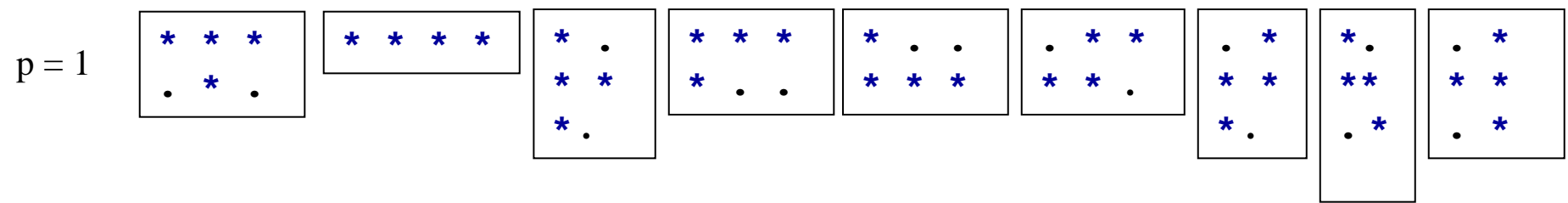
# Petits agrégats...

$$F_n = -kT \ln \left( \sum_p g_n^p e^{-E_n^p / kT} \right)$$

$p=0$



$$E_4^0 = 4E_{\text{ads}} + 4V_{\text{AA}}, \quad g_4^0 = 1$$



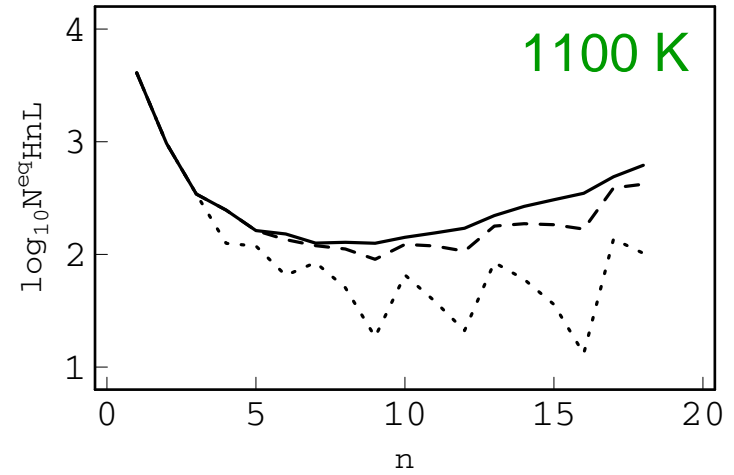
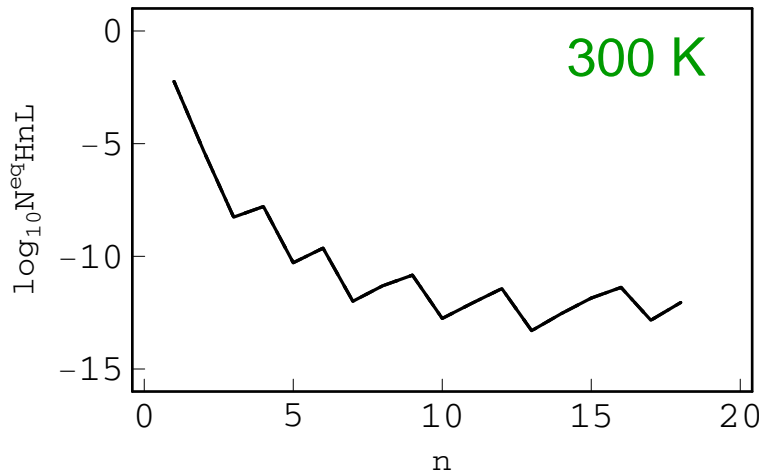
$$E_4^1 = 4E_{\text{ads}} + 3V_{\text{AA}},$$

$$g_4^1 = 18$$

$$g_{21}^{12} = 25\,424\,079\,339 \quad !!!$$

Pour les petites tailles détermination exacte de  $\Delta F_n$

# Compétition énergie / entropie

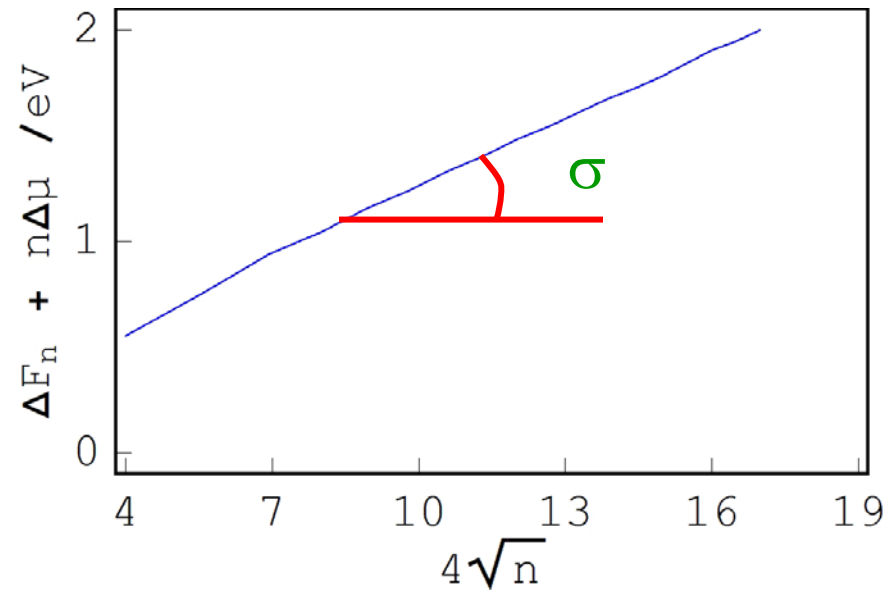


## Nombres magiques

### Détermination de $\sigma$

$$\frac{C_n}{D_n} = \exp\left(-\frac{\Delta F_n}{kT}\right)$$

$$\Delta F_n = -n\Delta\mu + 4\sqrt{n} \sigma + \sigma'$$



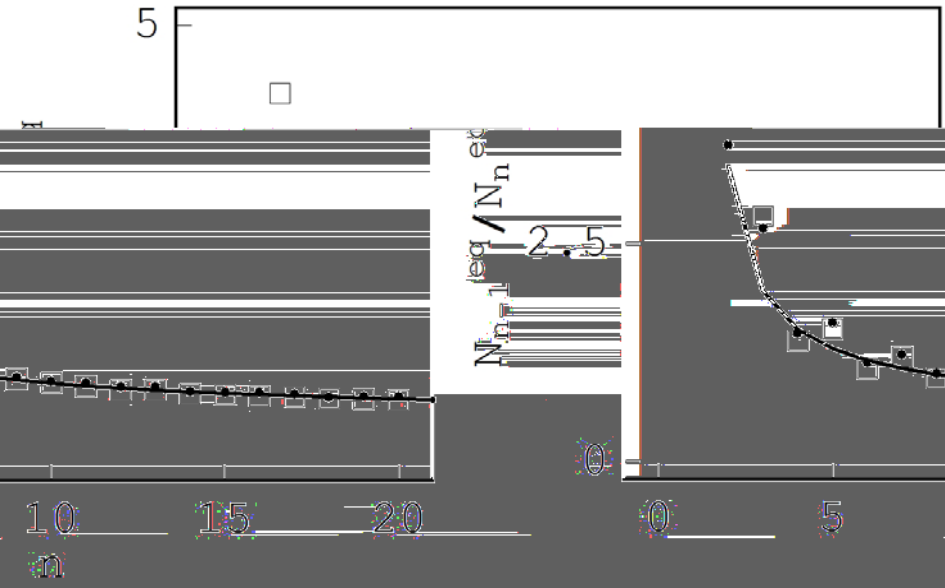
# Energie libre de surface des agrégats



$$\beta_n \propto \sum_i N_n^{iL,ads} \exp\left(-\frac{iV_{AA}}{2kT}\right)$$

$$\alpha_n \propto \sum_i N_n^{iL,des} \exp\left(\frac{iV_{AA}}{2kT}\right)$$

Vérification du bilan détaillé



détermination de  $\sigma$  :

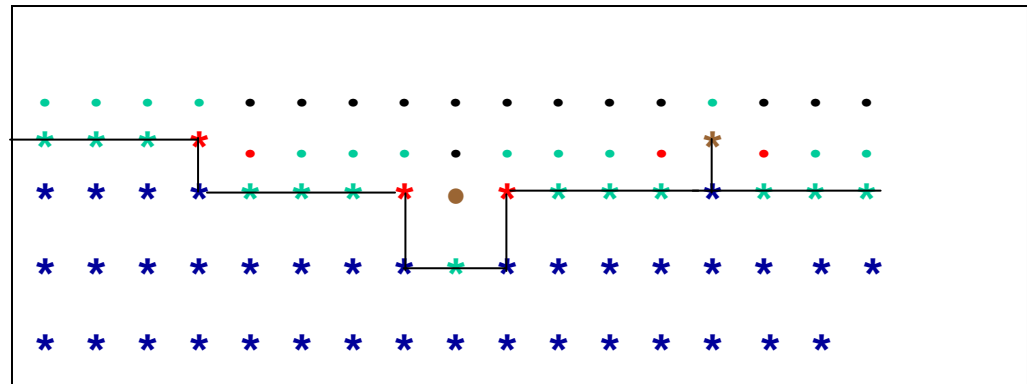
$$\sigma = -\frac{V_{AA}}{8(\sqrt{n+1} - \sqrt{n})} + \frac{kT}{4(\sqrt{n+1} - \sqrt{n})} \ln \left[ \frac{\sum_{i=1}^{Z-1} N_n^{iL,des} \exp\left(\frac{iV_{AA}}{2kT}\right)}{\sum_{i=1}^{Z-1} N_{n-1}^{iL,ads} \exp\left(-\frac{iV_{AA}}{2kT}\right)} \right]$$

$$\left( N_n^{iL,ads}, N_n^{iL,des} \right) = ???$$



# Champ moyen de lisière

- 1L désorption : \*
- 2L désorption : \*
- 3L désorption : \*
- 1L adsorption : •
- 2L adsorption : •
- 3L adsorption : •



$$N^{3L,ads} = N^{1L,des}, N^{2L,ads} = N^{2L,des}, N^{1L,ads} = N^{3L,des}$$

$$\frac{\partial F}{\partial N^{iL,des}} = 0$$

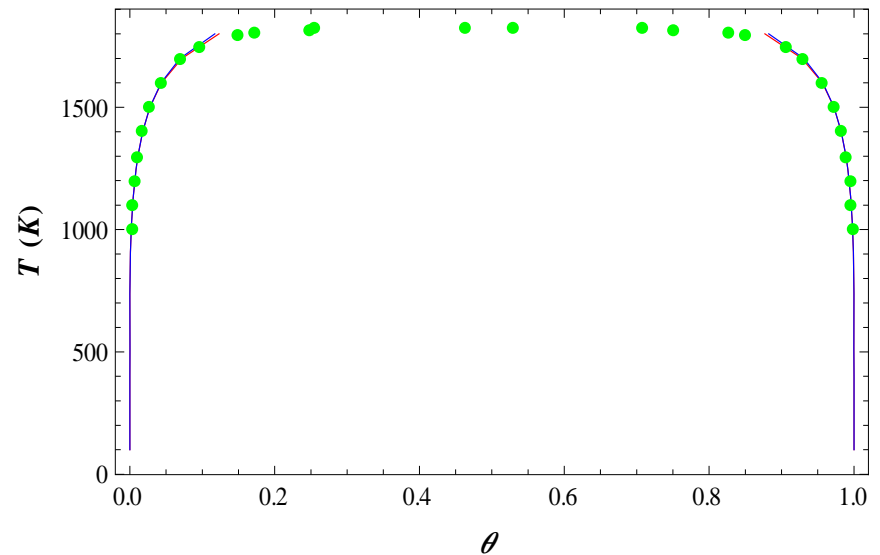
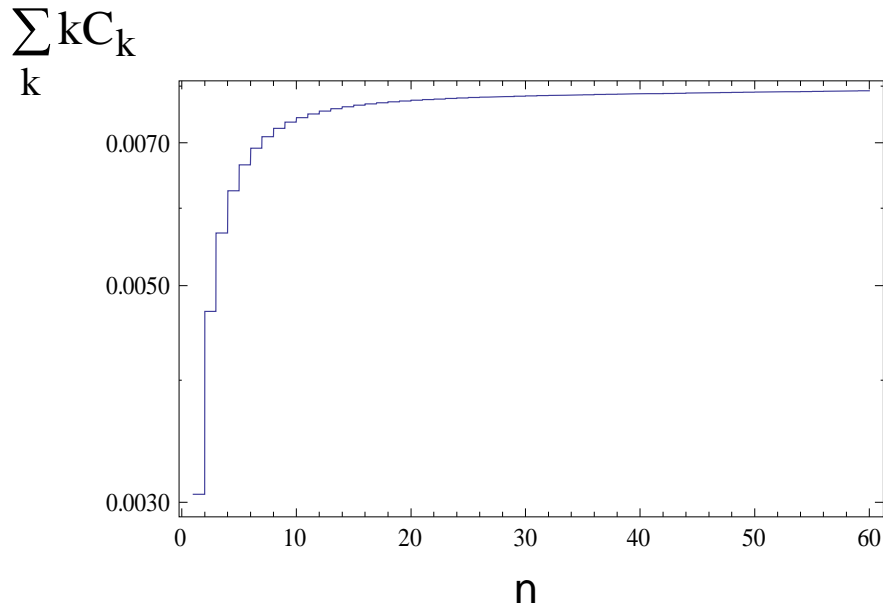
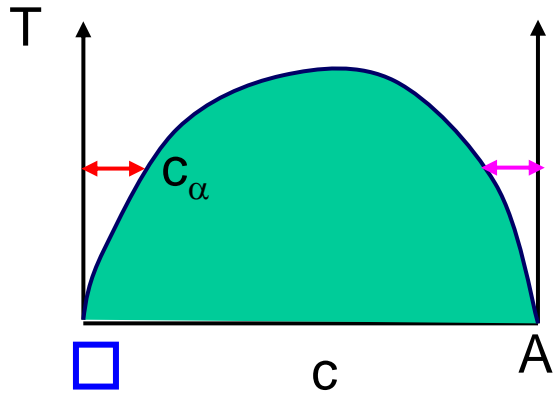
$$N_n^{2L,des} = 4\sqrt{n} \frac{r}{1+r+r^2/2}$$

$$r = 2 \exp\left(\frac{V_{AA}}{2kT}\right)$$

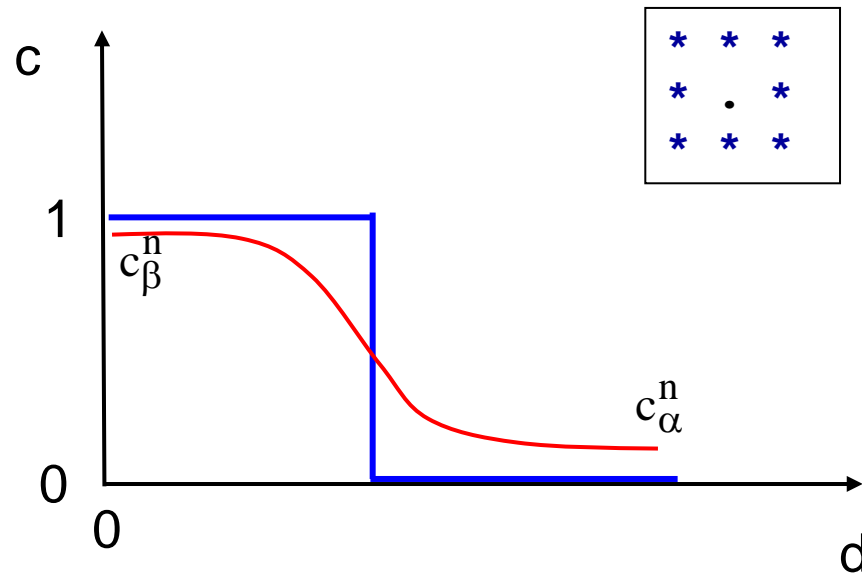
$$\sigma = -\frac{V_{AA}}{2} - kT \ln(1+r+r^2/2)$$

**Bon accord entre toutes les différentes valeurs de  $\sigma$  obtenues**

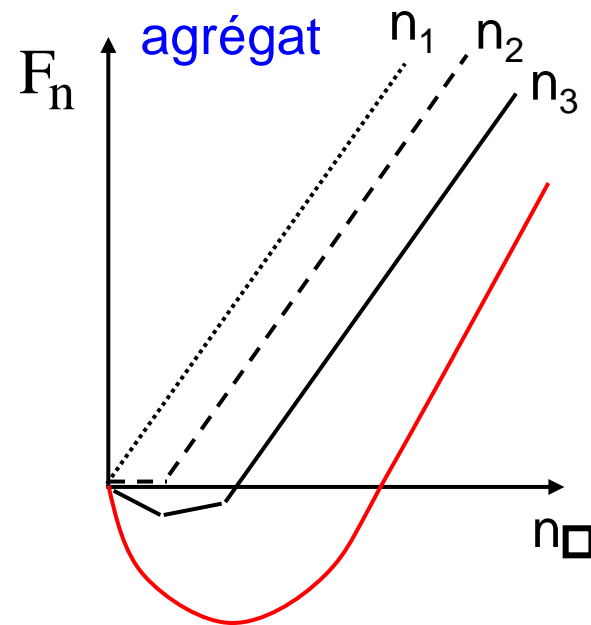
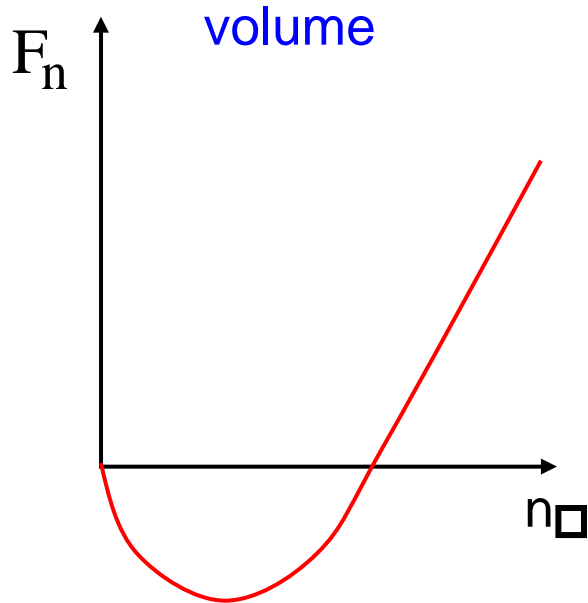
# *Liens entre $\sigma$ et le diagramme de phases*



# Quid des excitations de cœur ?



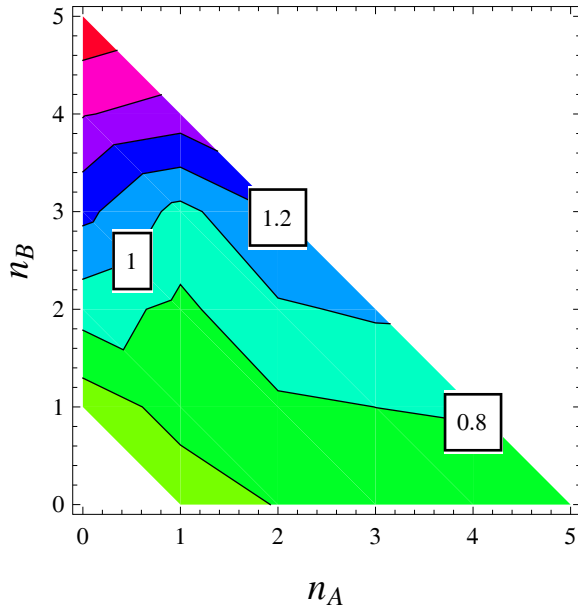
# Concentration de $\square$ dans un agrégat



**Compétition énergie / entropie**  
**Canonique / grand canonique... discret / continu**

# Agrégats bimétalliques

$$\Delta F(n_A, n_B)$$



discret et limité !

- ✓ système ternaire A-B-□
- ✓ Énergie libre de surface ?
- ✓ Taille critique de germination?
- ✓ Influence des lacunes dans les amas ?